



CSCI 2467, Fall 2017

Class Activity: Two's complement, bitwise and logical operators
Tuesday, September 5

1 Response Sheet Instructions

Please use these pages to record your group's answers. You can use the question pages as a workspace, then use this page for your final answers.

Names
Answer
Key

2 Review of Negative Integers

1. The leftmost bit of a *non-negative* number is always:

0

The leftmost bit of a *negative* number is always:

1

3. Write an expression (in terms of N) that gives the *most positive* number that can be represented by a N-bit two's complement number.

$$2^{N-1} - 1$$

2. Fill in the table below.

Bits	Most pos.	Most neg.
1	0	-1
2	1	-2
3	3	-4
4	7	-8

4. Write an expression (in terms of N) that gives the *most negative* number that can be represented by a N-bit two's complement number.

$$-2^{N-1}$$

All possible 3-bit values

000	0
001	1
010	2
011	3
100	-4
101	-3
110	-2
111	-1

3 Bit-level Operations

7. Fill in the table with your answers. Note the arrows showing the order of conversions in the table.

Hex.	Binary
$\sim(0xF0F0)$	$\sim(1111\ 0000\ 1111\ 0000)$
$0x0F0F$	$0000\ 1111\ 0000\ 1111$
$0x3C3C$	$0011\ 1100\ 0011\ 1100$
$0xC3C3$	$1100\ 0011\ 1100\ 0011$
$0xCAFE$	$1100\ 1010\ 1111\ 1110$
$0x3507$	$0011\ 0101\ 0000\ 0001$
$0x0000$	$0000\ 0000\ 0000\ 0000$
$0xFFFF$	$1111\ 1111\ 1111\ 1111$

8. Fill in the table using bitwise AND (&):

Dec	Bin	X & 0x1
-2	1110	0000
-1	1111	0001
0	0000	0000
1	0001	0001
2	0010	0000

9. For which numbers was the value ANDed with 0x1 not 0000? What is a common property of these integers?

-1 and 1
 both are odd numbers
 (last bit is a 1)

10. Explain the expression $(X \& \text{FLAG}) == \text{FLAG}$. When does it return true (1)? When does it return false (0)?

Returns true \rightarrow when any bit in FLAG is set in X

Returns false \rightarrow when NO bits set in FLAG are set in X

11. How is OR (|) used in the open() example?

OR (|) sets the relevant bits for each file access mode, combining those bits into one value (int) to be passed to open()

12. What constant value should you use as a bitmask in order to mask out all bits except the sign bit?

$\text{int signbit} = x \& \underline{0x80000000}$;

13. Provide an equivalent bitmask, but use a small constant and a shift instead of a large constant:

$\text{int signbit} = x \& \underline{1 \ll 31}$;

14. What is the value of signbit if x is positive? Negative?

If x is positive,
 $\text{signbit} == 0$

If x is negative
 $\text{signbit} == 0x80000000$

\downarrow which is the same as

TMin

15. Use a shift and a bitmask to convert signbit to either 0 (for positive) or 1 (for negative):

Could you also write this expression in terms of x?

```
int isNeg = ( signbit >> 31 ) & 0x1;
int isNeg = ( x >> 31 ) & 0x1;
```

or just 1
↓
0x1

4 Logical operations

1. With 4-bit values, how many values are false?

1 (zero is the only one)

How many are true?

15 (all non-zero values)

2. Evaluate the following expression:
(0x3 && 0xC) == (0x3 & 0xC)

Note: 4-bit numbers have 16 possible values

[&& is logical AND] ; [& is bitwise AND]
both 0x3 and 0xC are non-zero so they are both true, so this logical AND evaluates to 1

0x3 → 0011
0xC → 1100
0000 = 0

Is this result what you expected? Why or why not?

Expression simplifies to 1 == 0
Those two values are not equal, so that expression evaluates to false represented by 0

3. Test whether !!X == X holds across different values of X.

X	!X	!!X
-1	0	1
0	1	0
1	0	1
2	0	1

4. Using ~ instead of !:

X	~X	~~X
-1	0	-1
0	-1	0
1	-2	1
2	-3	2

How does this differ from the previous result? Why?

3 With ! there are only two possible results, 0 and 1.
~ has many possible results, in fact every unique int has a unique complement.
Also: ~(~(x)) == x is true (not for !)

Even though the two sides look almost identical, they are not equal. This could be surprising, until we know the difference between & and &&